

The DUNE PrismGrid Module

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Introduction

Design and Implementation of DUNE PrismGrid

Numerical Results and Applications

Conclusion

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Meta grids developed in Freiburg

- ▶ GeometryGrid (M. Nolte)
- ▶ IdGrid (M. Nolte)
- ▶ ParallelGrid (R. Klöfkorn)
- ▶ PrismGrid

Observations

- ▶ Easy to implement (?)
- ▶ Performance loss

Meta grids developed in Freiburg

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Project History

- ▶ First version developed in 2008 (*2D unstructured simplex grids to 3D prismatic grid, suitable for parallel computations*)
- ▶ New generic version since 2009
- ▶ Project website launch in 2010
- ▶ For 2011: make module available

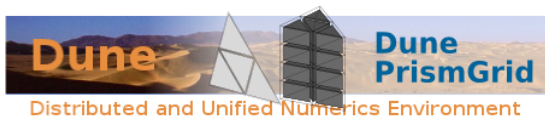


Figure: The DUNE PrismGrid logo

Features

- ▶ Generic prismatic elements over arbitrary d -dimensional DUNE grid (*the host grid*)
- ▶ Structured in vertical direction with flat upper and lower boundaries
- ▶ Periodic in vertical direction and horizontal directions (*if host grid is periodic*)
- ▶ Access to host grid

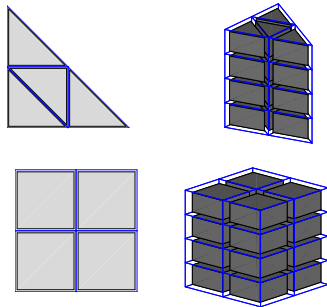


Figure: 2d host grids and resulting 3d prismatic grids

Features

- ▶ Access to several iterators for columns and layers
- ▶ Entities of all codimensions (*independent of the host grid implementation*)
- ▶ DGF support (*including IntervalBlock*)
- ▶ Two geometry implementations (*original implementation and generic geometries*)

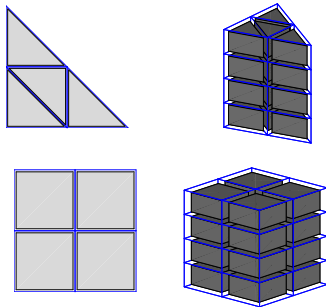


Figure: 2d host grids and resulting 3d prismatic grids

Open Issues

- ▶ Adaptivity
- ▶ Parallel support
- ▶ I/O
- ▶ Performance

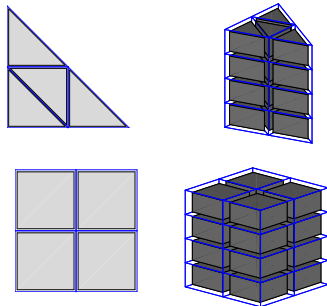


Figure: 2d host grids and resulting 3d prismatic grids

- ▶ New in DUNE 2.0: Generic reference elements
- ▶ Inductive construction rule (*pyramids and prisms*)
- ▶ In PrismGrid: Allows generic mapping from PrismGrid geometry types to host grid geometry types
- ▶ Generic Geometries

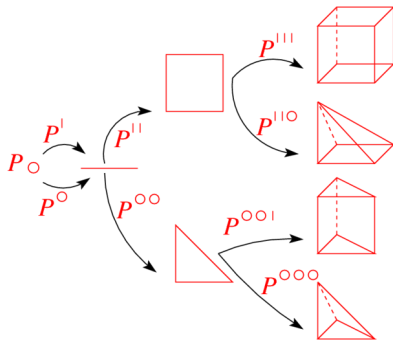


Figure: Construction of reference elements (A. Dedner)

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```

template< class HostGrid >
class PrismGrid
: GridDefaultImplementation < .. >
{
    ...

    // dimension of grid
    enum { dimension = HostGrid::dimension + 1 };

    // dimension of world
    enum { dimensionworld = HostGrid::dimensionworld + 1 };

    // constructor
    PrismGrid ( HostGrid * hostgrid, LineGrid * linegrid );

    // export type of underlying host grid
    typedef typename GridFamily::HostGrid HostGrid;
    HostGrid * hostGrid_;

    // type of line grid
    typedef typename GridFamily::LineGrid LineGrid;
    LineGrid * lineGrid_;

    ...
};

```

A LineGrid is a container of intervals with iterators and geometry:

```

template< class ctype >
class LineGrid
{
    // constructor
    LineGrid ( const int n, const ctype left, const ctype right,
              ...
              );

    // return iterator for given direction
    IteratorType iterator ( int direction ) const
    {
        if ( direction == 1 )
            return up_iterator();
        else
            return down_iterator();
    }

    // return end iterator for given direction
    IteratorType end_iterator ( int direction ) const;

    ...
};

```

A PrismGrid can be constructed from a DGF-file of the following form:

DGF

HOSTGRID

hostgrid.dgf % host grid dgf file

#

LINEGRID

0. 1. 2 % [0., 1.], 2 cells

55 66 % bottomId = 55, topId = 66

0 % no periodicity

#

The following GRIDTYPE typedefs are defined during `./configure`:

```
PRISMGRID_SGRID  
PRISMGRID_YASPGRID  
PRISMGRID_ONEDGRID  
PRISMGRID_ALBERTA  
PRISMGRID_ALUGRID_CONFORM  
PRISMGRID_ALUGRID_CUBE  
PRISMGRID_ALUGRID_SIMPLEX
```

Compile:

```
make GRIDTYPE=PRISMGRID_SGRID GRIDDIM=3 WORLDDIM=4 ...  
// host grid is SGRID< 2, 3 >
```

There are several possible iterators:

- ▶ Columnwise
- ▶ Layerwise
- ▶ From lower to upper
- ▶ From upper to lower

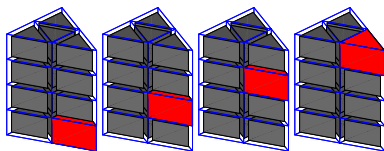


Figure: Iteration upwards a column

Which iterator shall be implemented / used / chosen?

There are several possible iterators:

- ▶ Columnwise
- ▶ Layerwise
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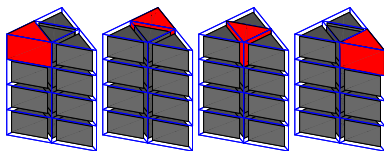


Figure: Iteration over top layer

Which iterator shall be implemented / used / chosen?

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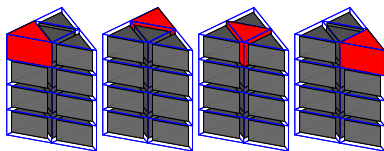


Figure: Iteration over top layer

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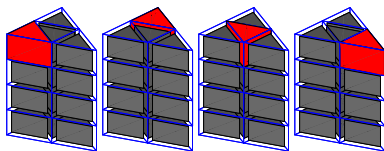


Figure: Iteration over top layer

Which iterator shall be implemented / used / chosen?

```

template< ... >
struct PrismGridSettings
{
    // define the iteration implementation to be used
    static const prismgrid::PrismGridIteratorImplementation
        IteratorImplementation = prismgrid::ColumnWise;
        // IteratorImplementation = prismgrid::LayerWise;

    // define the geometry implementation to be used
    static const prismgrid::PrismGridGeometryImplementation
        GeometryImplementation = prismgrid::OriginalGeometry;
        // GeometryImplementation = prismgrid::GenericGeometry;

    ...
};
  
```

- ▶ In many applications, the meta grid and the host grid are used simultaneously.
- ▶ The `HostGridAccess` structure makes the host grid available through the meta grid and gives access to host grid entities from meta grid entities.
- ▶ Meta grids implementing the host grid access: `GeometryGrid`, `IDGrid`, `PrismGrid`, ...

```

template< class HostGrid >
struct HostGridAccess< PrismGrid< HostGrid > >
{
    ...

    // return reference to host grid
    static const HostGrid & hostGrid ( const PrismGrid & grid )
    {
        return grid.hostGrid();
    }

    // get host grid entity
    template< class Entity >
    static const typename Codim< Entity::codimension >::HostEntity &
    hostEntity ( const Entity &entity );

    ...
};

```

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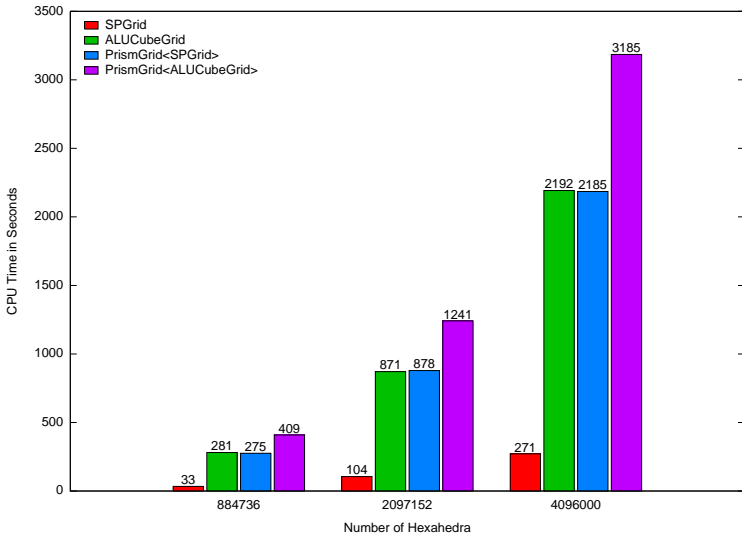
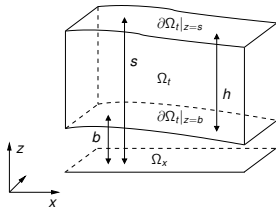


Chart provided by M. Nolte

- ▶ Geometry: Copy $d \times d$ -FieldMatrix into $(d + 1) \times (d + 1)$ -FieldMatrix for JacobianTransposed, JacobianInverseTransposed, ...
- ▶ Methods returning references
- ▶ Hold as few entity pointers as possible!

We consider the d -dimensional incompressible Navier-Stokes equations for shallow flows with a free surface ($d = 2, 3$):

$$\begin{aligned}
 \partial_t u_x + (u \cdot \nabla) u_x + \nabla_x p &= \mu \partial_z^2 u_x && \text{in } \Omega_t, \\
 \nabla \cdot u &= 0 && \text{in } \Omega_t, \\
 \partial_z p &= -g && \text{in } \Omega_t, \\
 \partial_t s + u_x \cdot \nabla_x s &= u_z && \text{on } \partial\Omega_t|_{z=s}, \\
 u_x \cdot \nabla_x b &= u_z && \text{on } \partial\Omega_t|_{z=b}, \\
 \mu \partial_z u_x &= 0 && \text{on } \partial\Omega_t|_{z=s}, \\
 \mu \partial_z u_x &= \kappa u_x && \text{on } \partial\Omega_t|_{z=b}.
 \end{aligned}$$



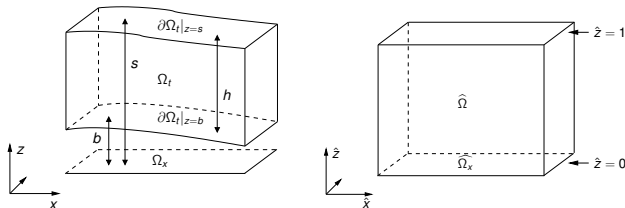
For the discretization, the so called σ -transformation is applied: Let

$$\hat{t} = t, \quad \hat{x} = x, \quad \text{and} \quad \hat{z} = \sigma(t, x, z) = \frac{z - b(x)}{h(t, x)}.$$

Then, for all times t it holds

$$\widehat{\Omega}_t = \{(\hat{x}, \hat{z}) \mid (x, z) \in \Omega_t\} = \widehat{\Omega}_x \times (0, 1),$$

i. e. the transformed domain is fixed in time.



- ▶ LDG solver in DUNE-FEM
- ▶ used an early version of PrismGrid
- ▶ combination of PrismGrid and GeometryGrid for visualization

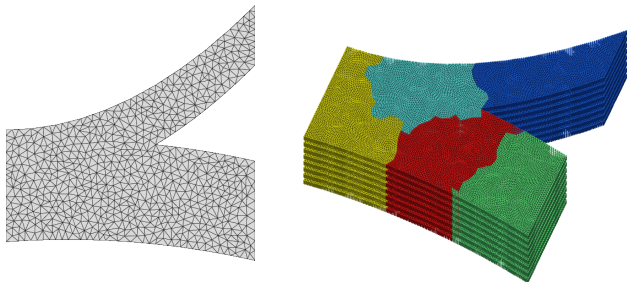


Figure: Two dimensional unstructured simplex grid (left) and resulting three dimensional prismatic grid with five partitions for parallel computations (right)

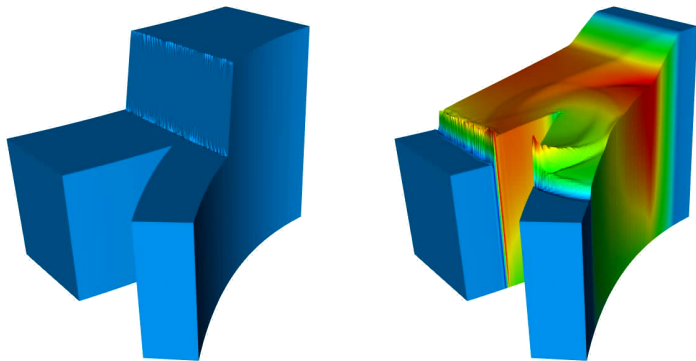


Figure: (Left) 3D representation of initial conditions and (Right) solution to a latter time

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- ▶ PrismGrid: meta grid with prismatic elements and additional functionality (*iterators, host grid acces*)
- ▶ Importance of generic reference elements for meta grids

Outlook

- ▶ Parallelization
- ▶ Adaptivity
- ▶ Performance
- ▶ Documentation
- ▶ ...

Thank you for your attention!

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